## Set Symbols

A set is a collection of things, usually numbers. We can list each element (or "member") of a set inside curly brackets like this:


## Common Symbols Used in Set Theory

Symbols save time and space when writing. Here are the most common set symbols In the examples $C=\{1,2,3,4\}$ and $D=\{3,4,5\}$

| Symbol | Meaning | Example |
| :---: | :---: | :---: |
| \{ \} | Set: a collection of elements | \{1,2,3,4\} |
| $A \cup B$ | Union: in A or B (or both) | $C \cup D=\{1,2,3,4,5\}$ |
| $A \cap B$ | Intersection: in both $A$ and $B$ | $C \cap D=\{3,4\}$ |
| $A \subseteq B$ | Subset: A has some (or all) elements of B | $\{3,4,5\} \subseteq D$ |
| $A \subset B$ | Proper Subset: A has some elements of B | $\{3,5\} \subset D$ |
| $A \not \subset B$ | Not a Subset: $A$ is not a subset of $B$ | $\{1,6\} \not \subset C$ |
| $A \supseteq B$ | Superset: A has same elements as B, or more | $\{1,2,3\} \supseteq\{1,2,3\}$ |
| $A \supset B$ | Proper Superset: A has B's elements and more | $\{1,2,3,4\} \supset\{1,2,3\}$ |
| $A \not \supset B$ | Not a Superset: $A$ is not a superset of $B$ | $\{1,2,6\} \not \supset\{1,9\}$ |
| $A^{C}$ | Complement: elements not in A | When $\begin{aligned} D^{C} & =\{1,2,6,7\} \\ \mathbb{U} & =\{1,2,3,4,5,6,7\}\end{aligned}$ |
| $A-B$ | Difference: in $A$ but not in $B$ | $\{1,2,3,4\}-\{3,4\}=\{1,2\}$ |
| $a \in \mathrm{~A}$ | Element of: $a$ is in A | $3 \in\{1,2,3,4\}$ |
| $b \notin \mathrm{~A}$ | Not element of: $b$ is not in A | $6 \notin\{1,2,3,4\}$ |
| $\emptyset$ | Empty set $=\{ \}$ | $\{1,2\} \cap\{3,4\}=\varnothing$ |
| $U$ | Universal Set: set of all possible values |  |


| $\mathbf{P}(\mathrm{A})$ | Power Set: all subsets of A | $\begin{gathered} P(\{1,2\})=\{\{ \},\{1\},\{2\}, \\ \{1,2\}\} \end{gathered}$ |
| :---: | :---: | :---: |
| $A=B$ | Equality: both sets have the same members | $\{3,4,5\}=\{5,3,4\}$ |
| $A \times B$ | Cartesian Product (set of ordered pairs from $A$ and $B$ ) | $\begin{gathered} \{1,2\} \times\{3,4\} \\ =\{(1,3),(1,4),(2,3),(2,4)\} \end{gathered}$ |
| $\|A\|$ | Cardinality: the number of elements of set $A$ | $\|\{3,4\}\|=2$ |
| 1 | Such that | $\{n \mid n>0\}=\{1,2,3, \ldots\}$ |
| : | Such that | $\{n: n>0\}=\{1,2,3, \ldots\}$ |
| $\forall$ | For All | $\forall x>1, x^{2}>x$ |
| $\exists$ | There Exists | $\exists x \mid x^{2}>x$ |
| $\therefore$ | Therefore | $a=b: b=a$ |
| $\mathbb{N}$ | Natural Numbers | $\{1,2,3, \ldots\}$ or $\{0,1,2,3, \ldots\}$ |
| $\mathbb{Z}$ | Integers | $\{\ldots,-3,-2,-1,0,1,2,3, \ldots\}$ |
| $\mathbb{Q}$ | Rational Numbers |  |
| A | Algebraic Numbers |  |
| $\mathbb{R}$ | Real Numbers |  |
| II | Imaginary Numbers | $3 i$ |
| C | Complex Numbers | $2+5 i$ |

